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# AC/DC/AC Converters: Two-Level and Multilevel VSI

*Josep Pou*  
*Antoni Arias*

# Outline

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- 1. Two-Level Inverter**
- 2. Multilevel Inverters**
  - Cascade H-Bridge Inverter**
  - Flying-Capacitor Inverter**
  - Diode-Clamped Inverter**
- 3. Back-to-Back Connection**

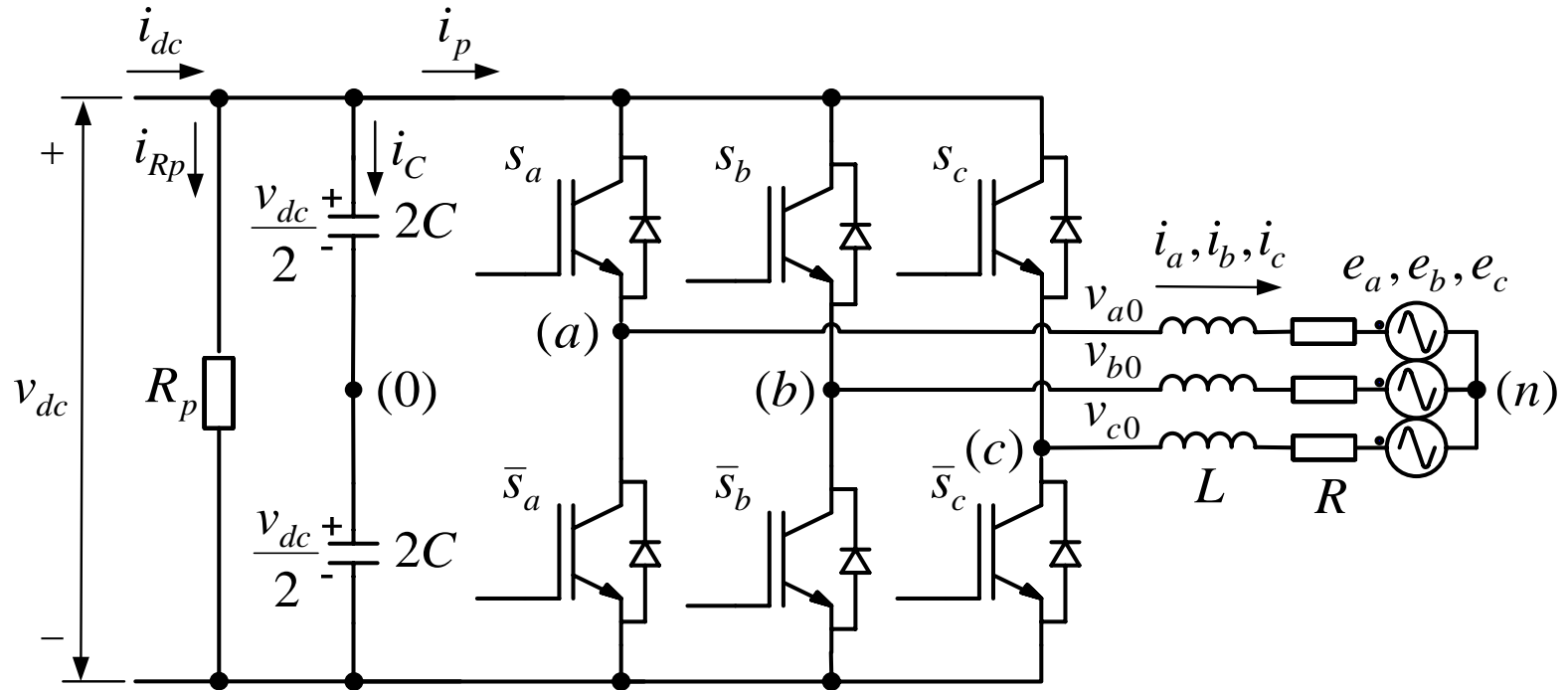
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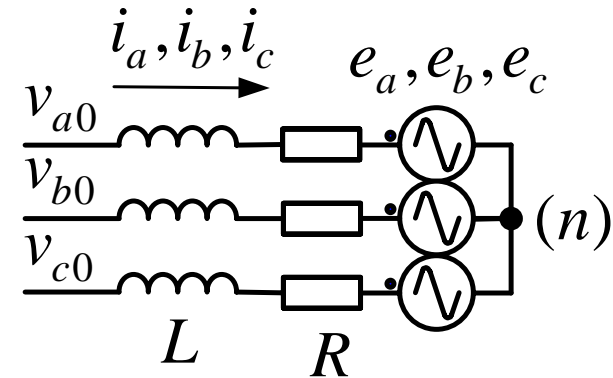
# 1. Two-Level Three-Phase Inverter

## Grid-connected inverter



# Modeling the AC Side

$$\begin{cases}
 v_{a0} = L \frac{di_a}{dt} + R i_a + e_a + v_{n0} \\
 v_{b0} = L \frac{di_b}{dt} + R i_b + e_b + v_{n0} \\
 v_{c0} = L \frac{di_c}{dt} + R i_c + e_c + v_{n0}
 \end{cases}$$



$$v_{a0} + v_{b0} + v_{c0} = L \frac{d(i_a + i_b + i_c)}{dt} + R(i_a + i_b + i_c) + e_a + e_b + e_c + 3v_{n0}$$

$$\Downarrow \quad i_a + i_b + i_c = 0$$

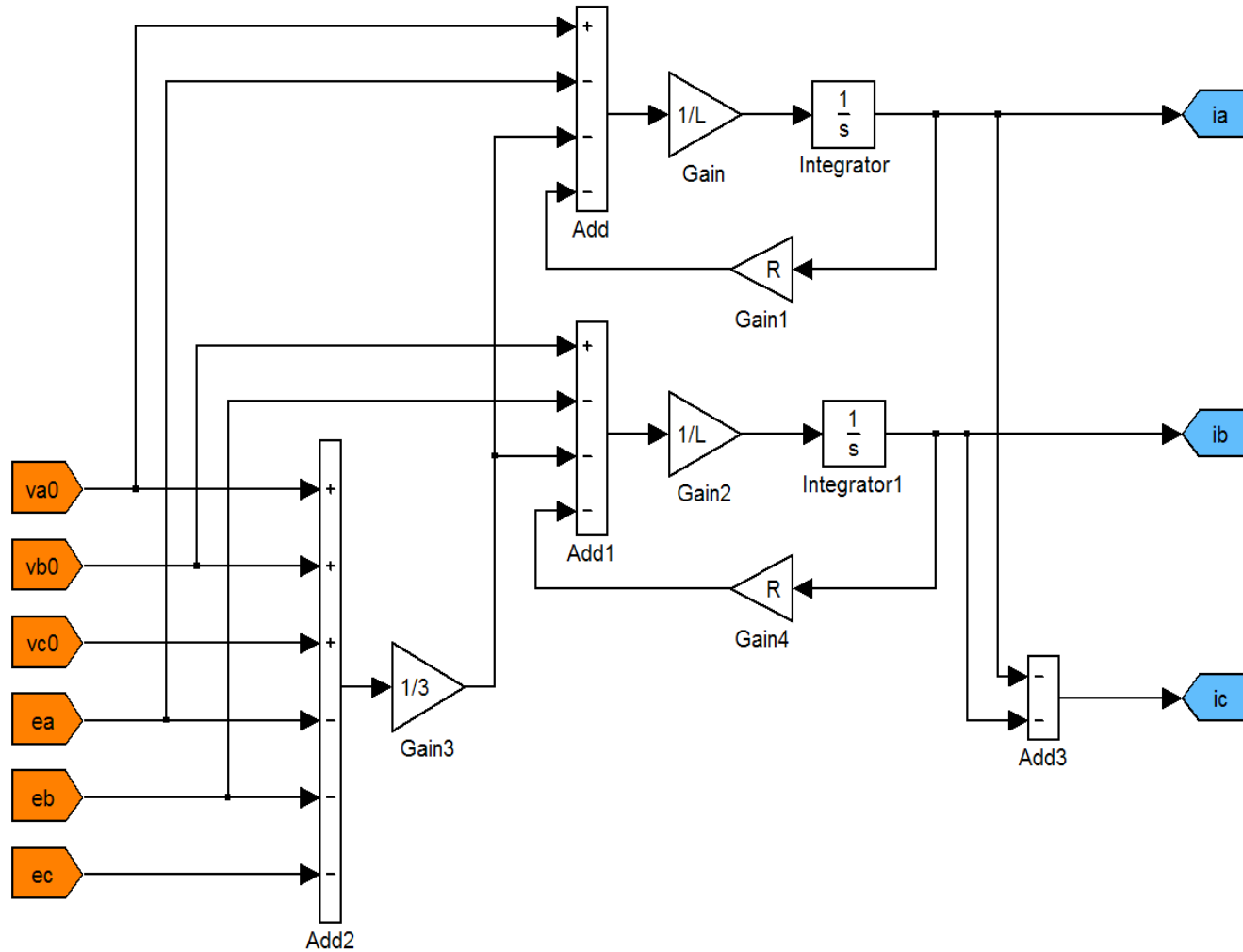
$$v_{n0} = \frac{v_{a0} + v_{b0} + v_{c0} - (e_a + e_b + e_c)}{3}$$

# Modeling the AC Side

$$\begin{cases} \frac{di_a}{dt} = \frac{1}{L} (v_{a0} - Ri_a - e_a - v_{n0}) \\ \frac{di_b}{dt} = \frac{1}{L} (v_{b0} - Ri_b - e_b - v_{n0}) \\ \frac{di_c}{dt} = \frac{1}{L} (v_{c0} - Ri_c - e_c - v_{n0}) \end{cases}$$

$$\begin{cases} i_a = \int di_a = \int \frac{1}{L} (v_{a0} - Ri_a - e_a - v_{n0}) dt \\ i_b = \int di_b = \int \frac{1}{L} (v_{b0} - Ri_b - e_b - v_{n0}) dt \\ i_c = -i_a - i_b \end{cases}$$

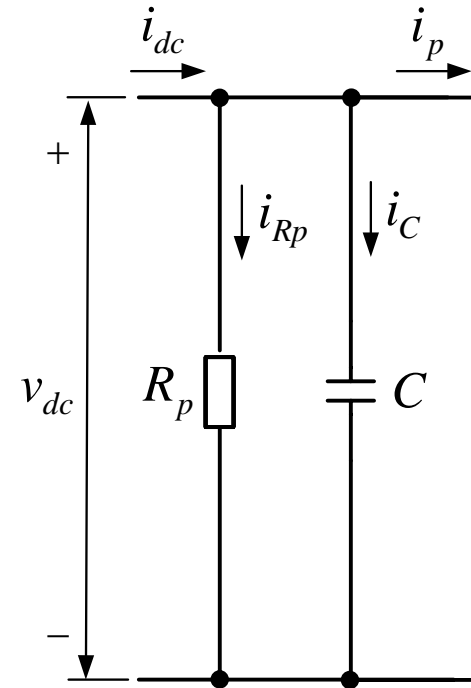
# Matlab-Simulink Model



# Modeling the DC Side

$$\begin{cases} i_C = i_{dc} - i_{Rp} - i_p = C \frac{dv_{dc}}{dt} \\ i_{Rp} = \frac{v_{dc}}{R_p} \end{cases}$$

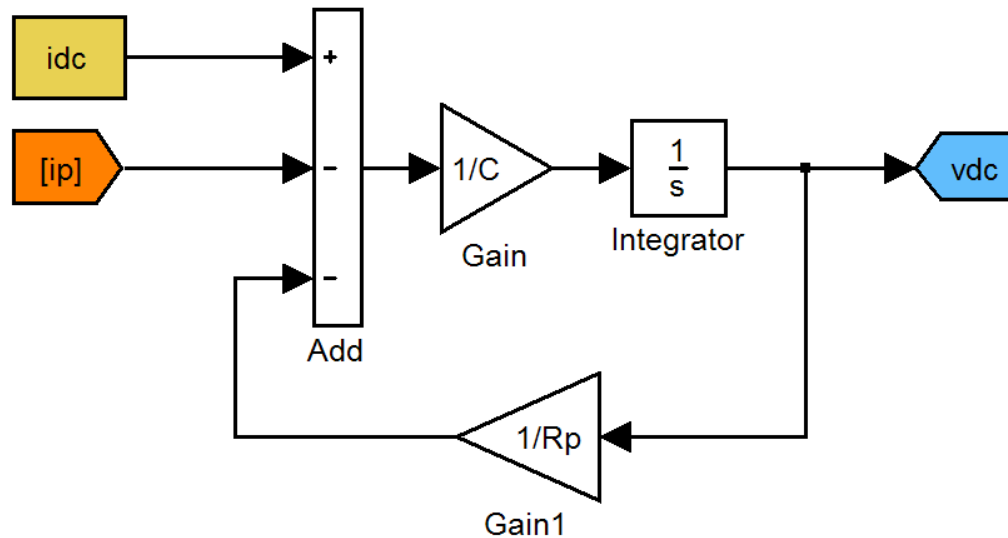
$$\frac{dv_{dc}}{dt} = \frac{1}{C} \left( i_{dc} - \frac{v_{dc}}{R_p} - i_p \right)$$



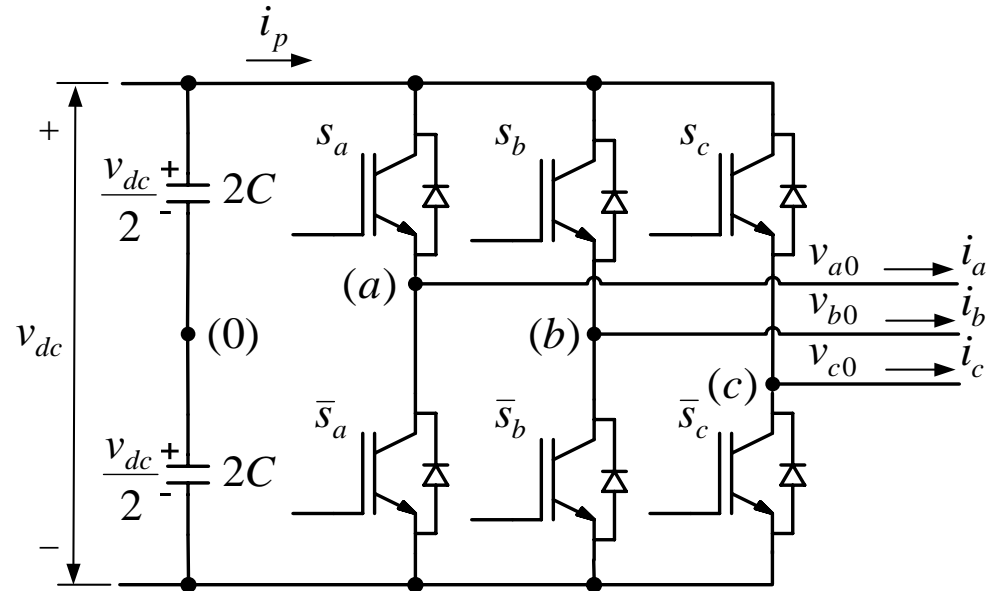


# Matlab-Simulink Model

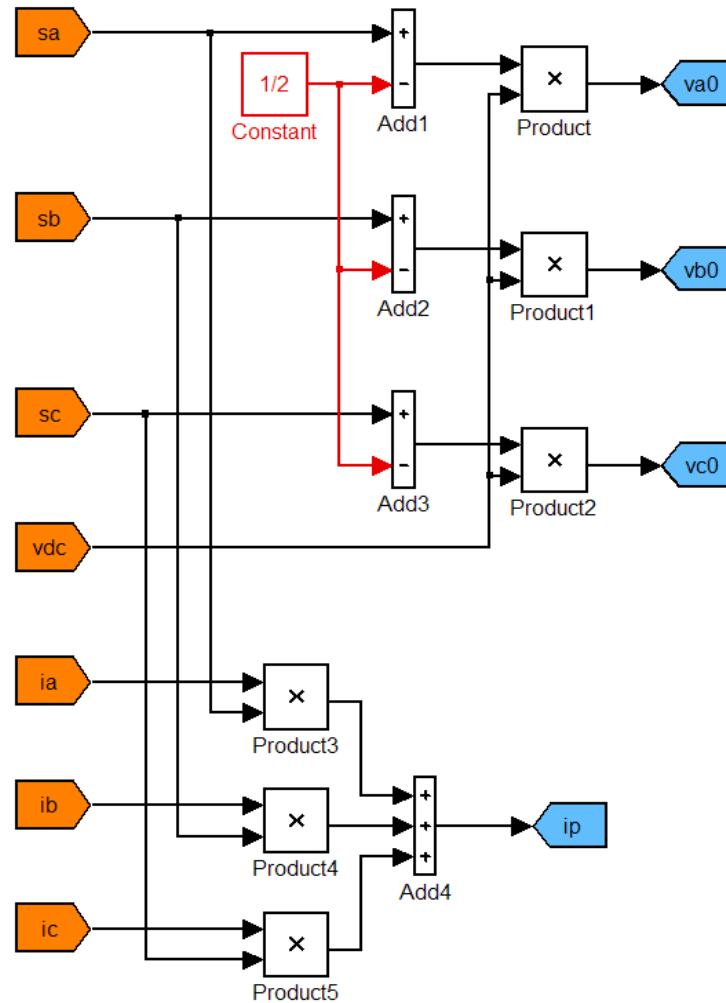
$$v_{dc} = \int dv_{dc} = \int \frac{1}{C} \left( i_{dc} - \frac{v_{dc}}{R_p} - i_p \right) dt$$



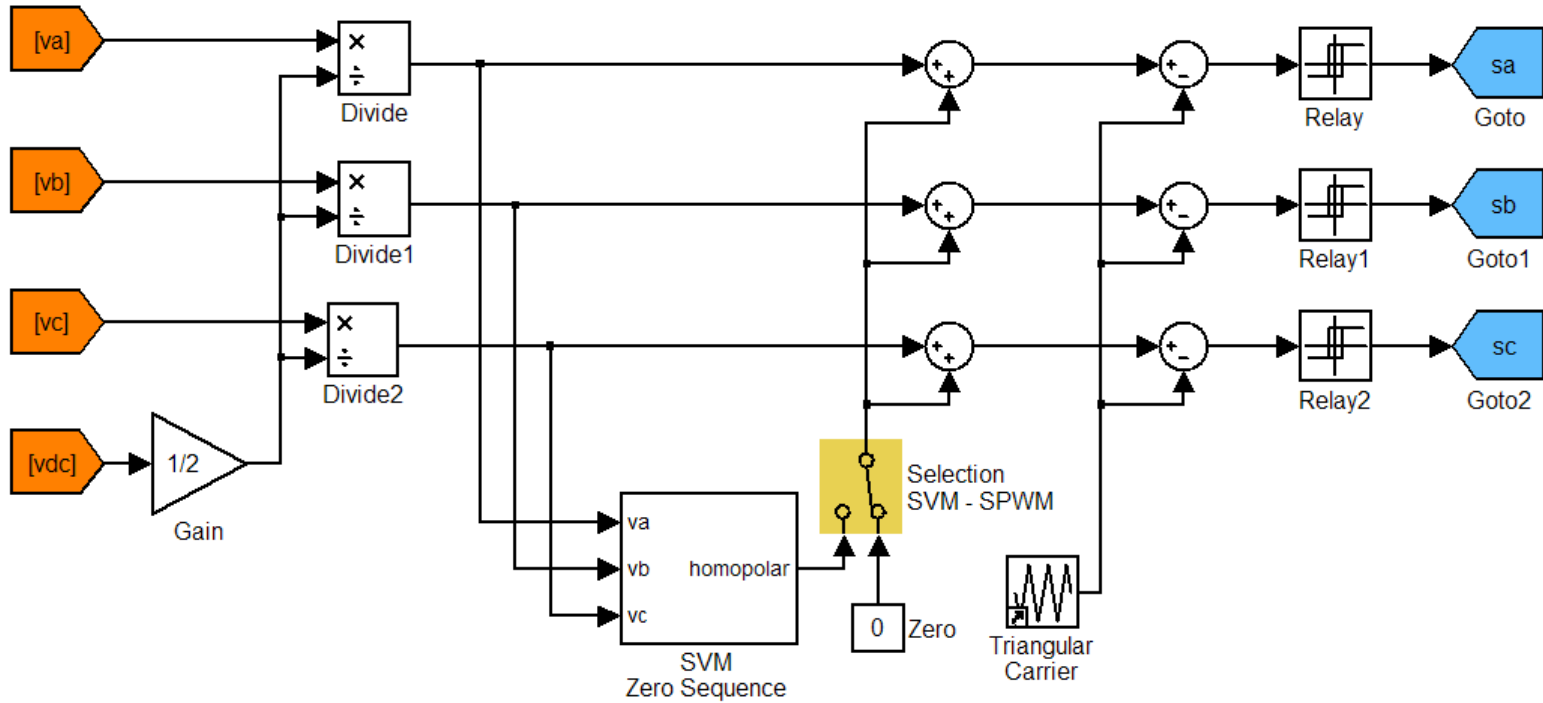
$$\begin{cases} v_{a0} = (s_a - \frac{1}{2})v_{dc} \\ v_{b0} = (s_b - \frac{1}{2})v_{dc} \\ v_{c0} = (s_c - \frac{1}{2})v_{dc} \\ i_p = s_a i_a + s_b i_b + s_c i_c \end{cases}$$



# Matlab-Simulink Model

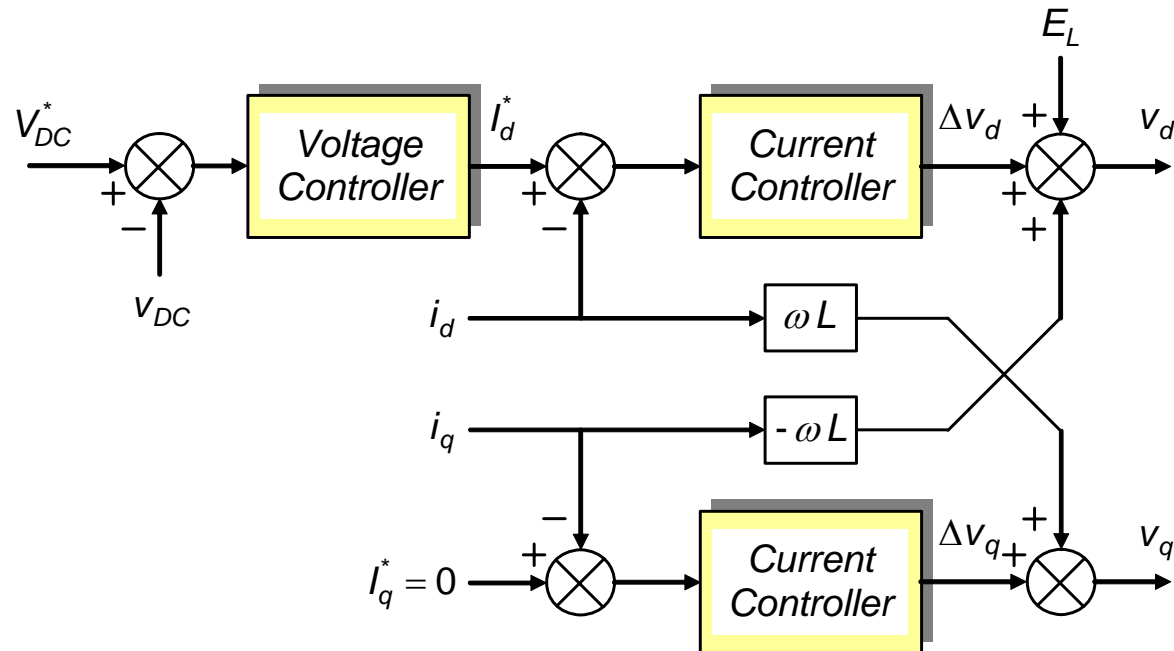


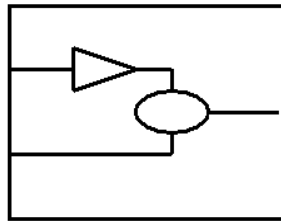
# Modulation (Sinusoidal PWM)



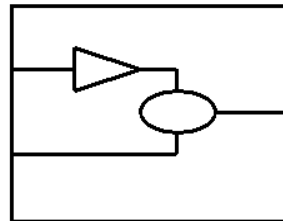
# Control

## Voltage Oriented Control (VOC)

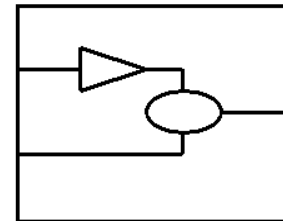




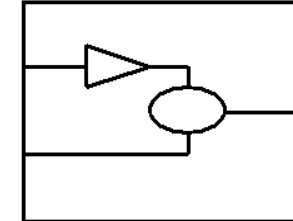
DC Side



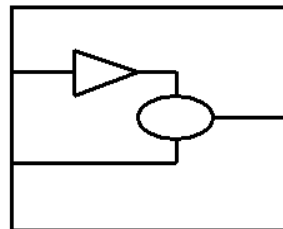
Converter



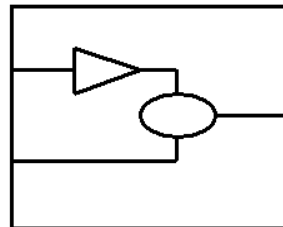
AC Side



Electrical Grid



Modulator

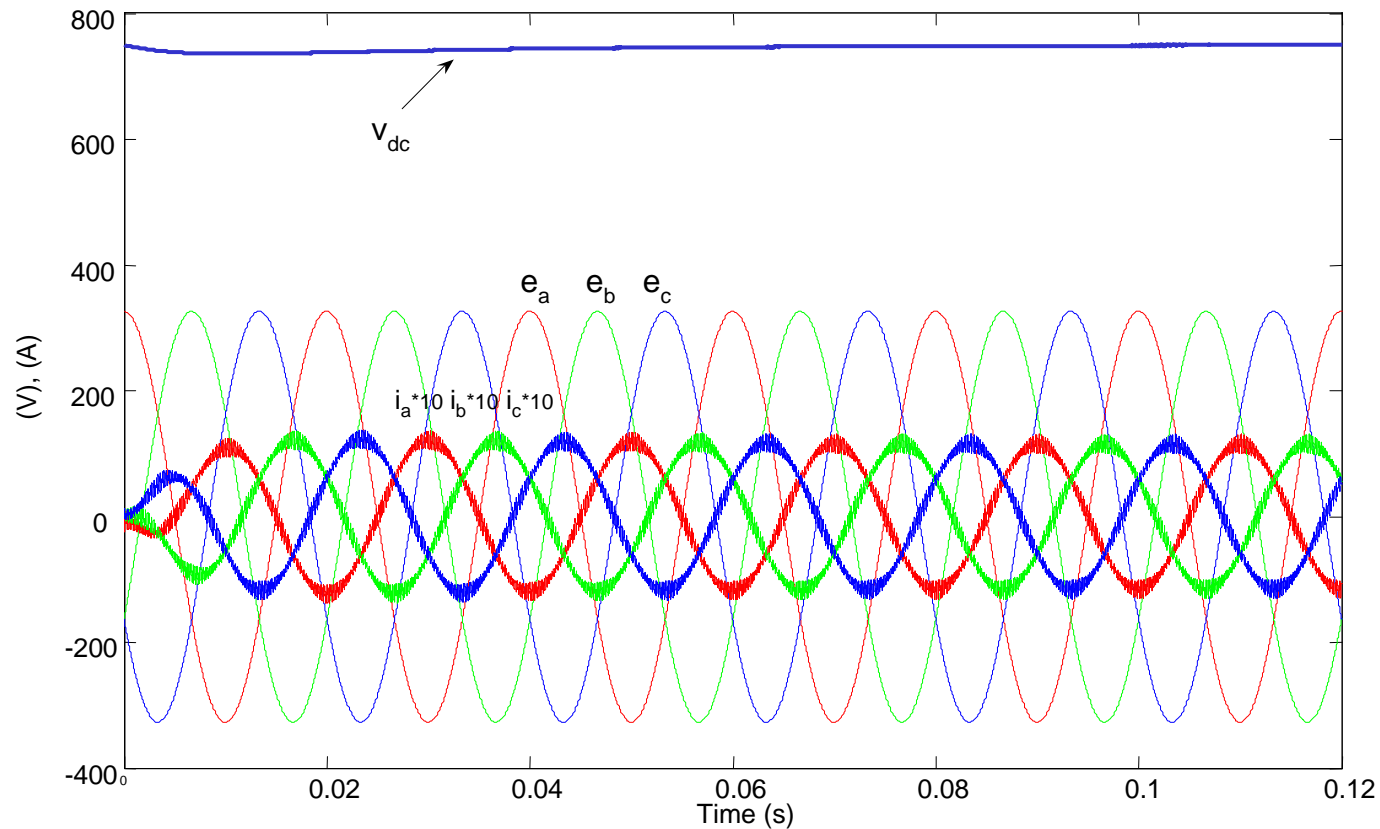


Control

# Simulation Results

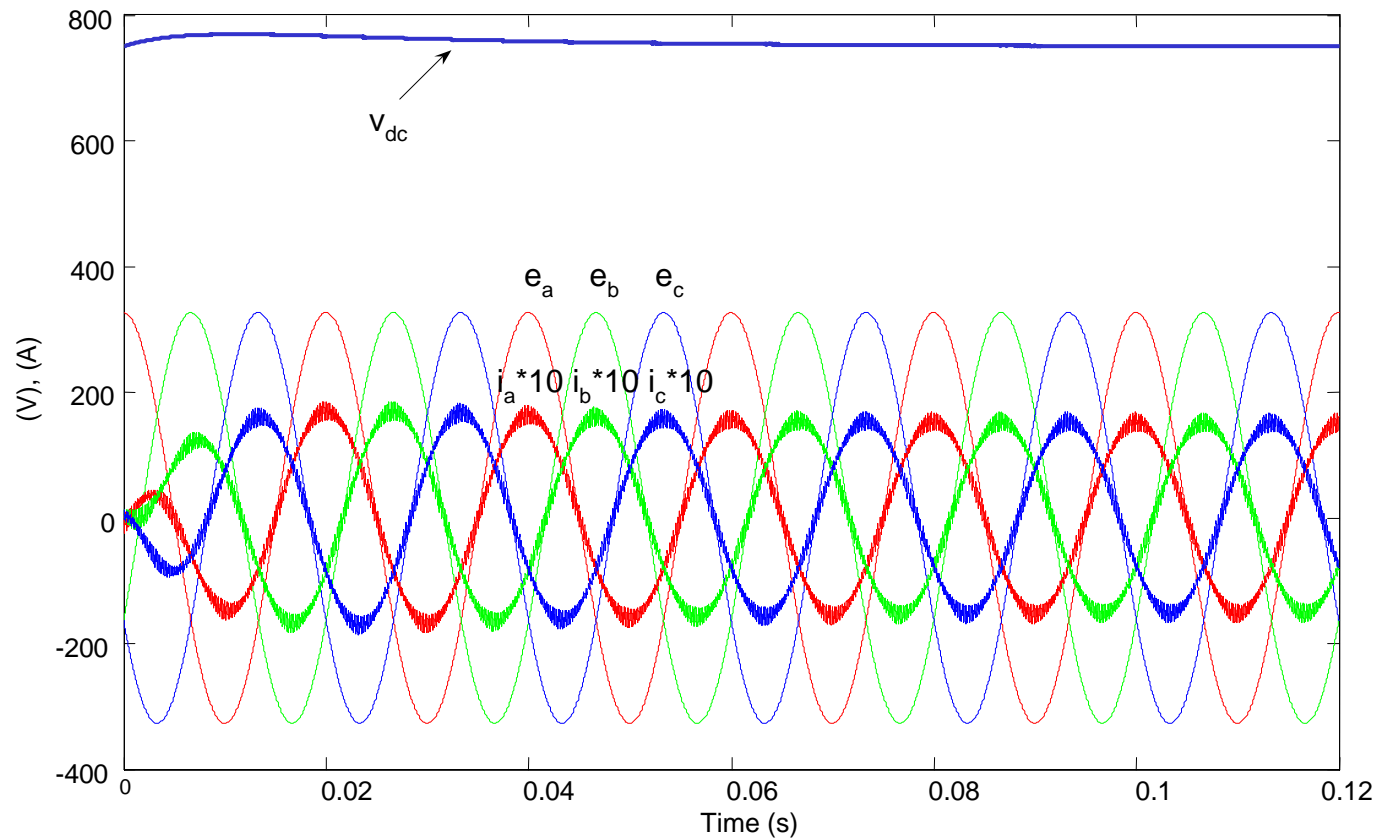
Main data:  $V_{LRMS}=400V$ ,  $f=50Hz$ ,  $L=6mH$ ,  $R=0.1\Omega$ ,  $C=2200\mu F$ ,  
 $V_{dc}^*=750 V$ ,  $f_s=5kHz$ .

Particular data:  $R_p=100\Omega$ ,  $I_{dc}=0$ ,  $I_q^*=0$



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 $V_{dc}^*=750 V$ ,  $f_s=5kHz$ .

Particular data:  $R_p=10k\Omega$ ,  $I_{dc}=10A$ ,  $I_q^*=0$

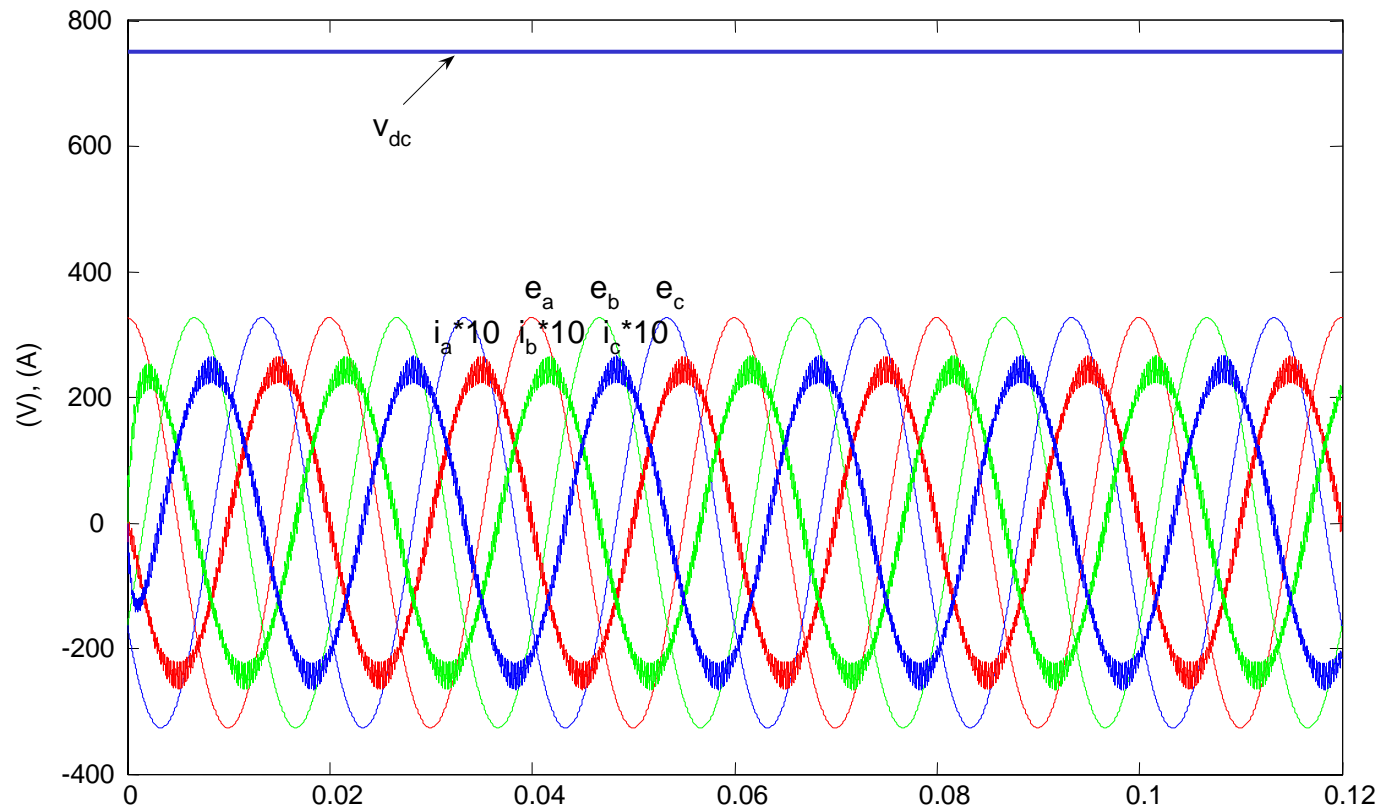




# Simulation Results

Main data:  $V_{LRMS}=400V$ ,  $f=50Hz$ ,  $L=6mH$ ,  $R=0.1\Omega$ ,  $C=2200\mu F$ ,  
 $V_{dc}^*=750 V$ ,  $f_s=5kHz$ .

Particular data:  $R_p=10k\Omega$ ,  $I_{dc}=0$ ,  $I_q^*=20A$



# Outline

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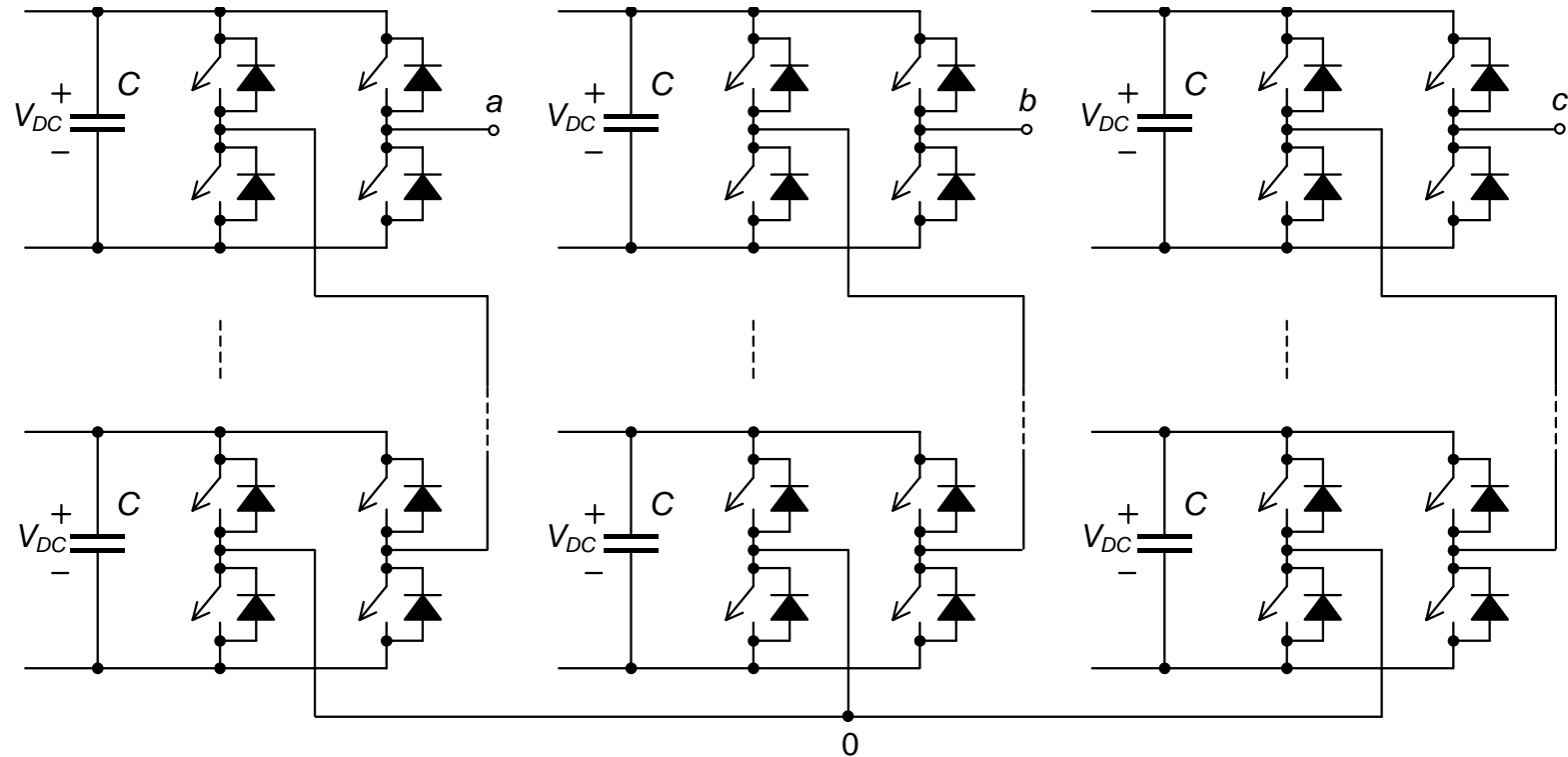
1. Two-Level Inverter
2. **Multilevel Inverters**
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## 2. Multilevel Inverters

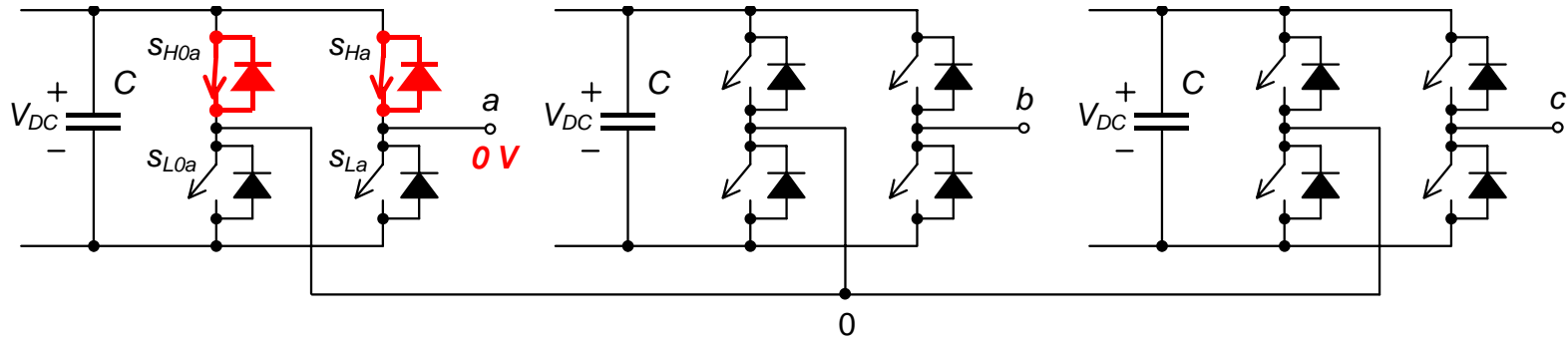
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- Multilevel inverters can provide more than two voltage levels at the outputs.
- Main advantages compared with the two-level inverter:
  - high quality of the output voltage spectra and
  - larger voltages that can be handled.
- Suitable for high-power applications.
- Main multilevel topologies:
  - (1) cascade H-bridge inverter,
  - (2) floating-capacitor inverter, and
  - (3) diode-clamped inverter.

# (1) Cascade H-Bridge Inverters



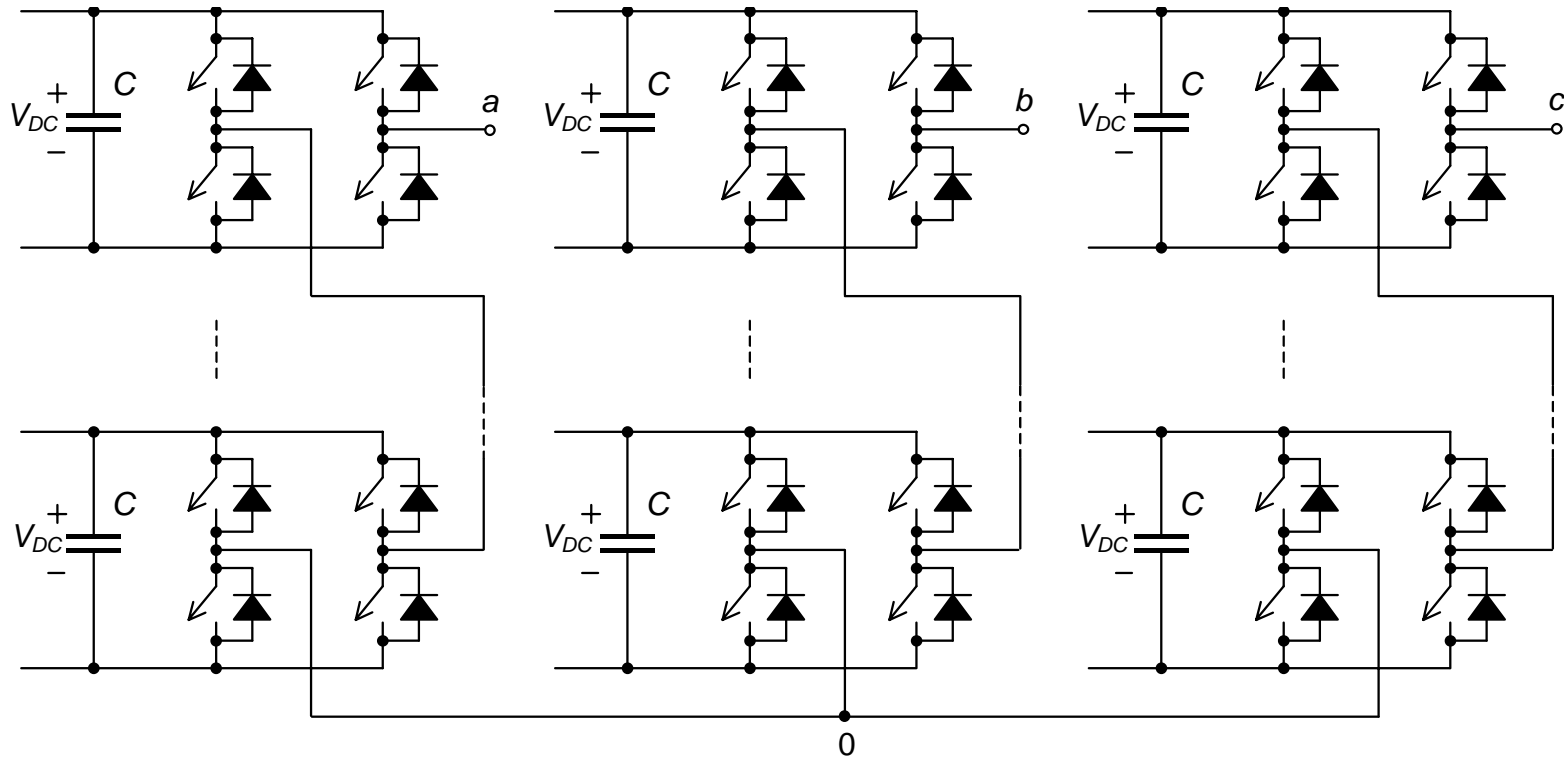
# Three-Level Basic Structure



Control functions:  $s_{H0a}$  and  $s_{Ha}$

$s_{H0a}$	$s_{Ha}$	$V_{a0}$
<i>off</i>	<i>off</i>	<b>0</b>
<i>off</i>	<i>on</i>	<b><math>+V_{DC}</math></b>
<i>on</i>	<i>off</i>	<b><math>-V_{DC}</math></b>
<i>on</i>	<i>on</i>	<b>0</b>

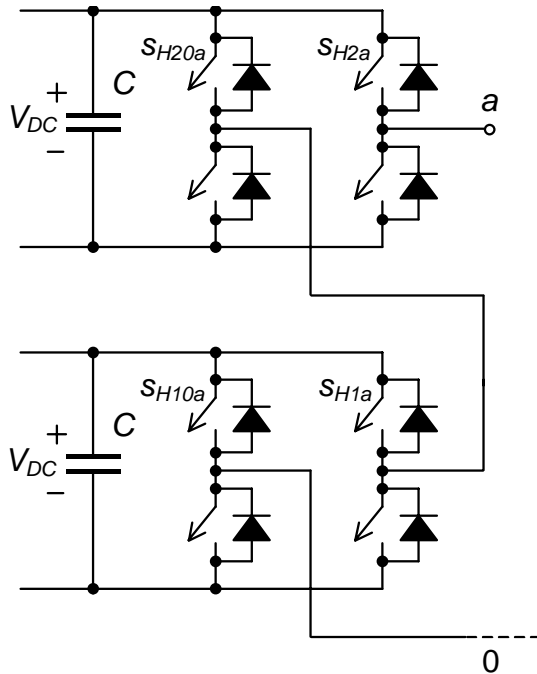
# Even Number of Levels



$$n = 2h + 1$$

$n$ : number of output levels (per phase)  
 $h$ : number of cascaded H cells

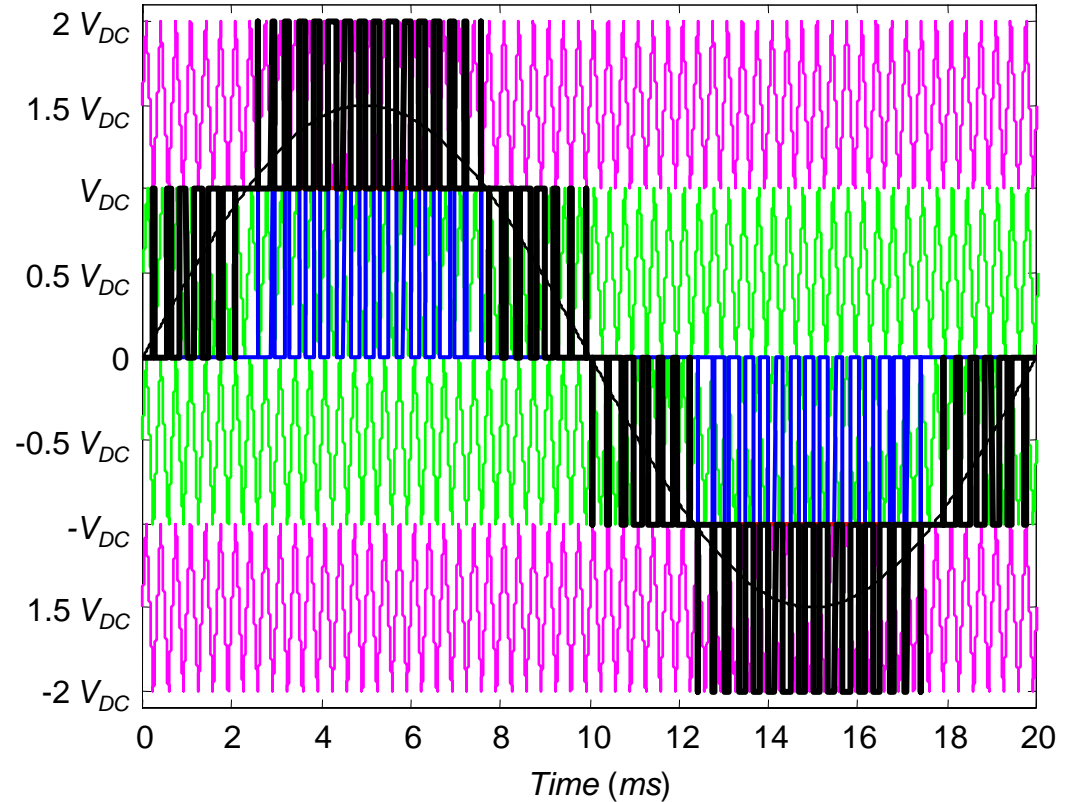
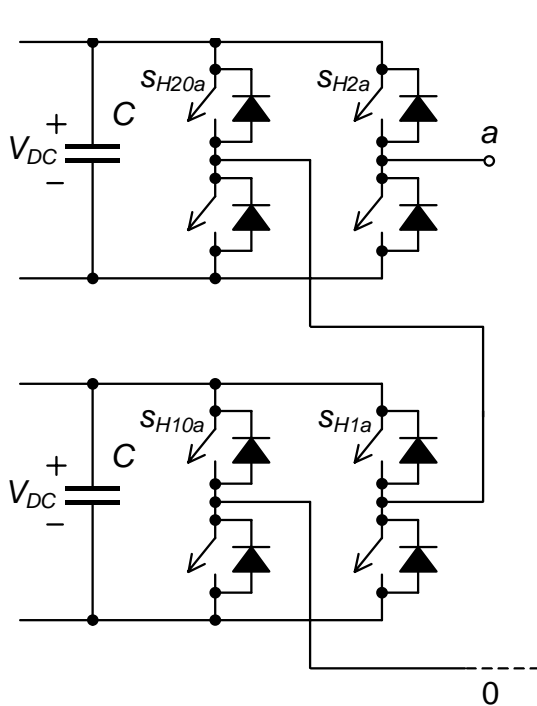
# Cascaded Five-Level Inverter



$S_{H20a}$	$S_{H2a}$	$S_{H10a}$	$S_{H1a}$	$V_{a0}$
off	off	off	off	<b>0</b>
off	off	off	on	$+V_{DC}$
off	off	on	off	$-V_{DC}$
off	off	on	on	<b>0</b>
off	on	off	off	$+V_{DC}$
off	on	off	on	$+2V_{DC}$
off	on	on	off	<b>0</b>
off	on	on	on	$+V_{DC}$
on	off	off	off	$-V_{DC}$
on	off	off	on	<b>0</b>
on	off	on	off	$-2V_{DC}$
on	off	on	on	$-V_{DC}$
on	on	off	off	<b>0</b>
on	on	off	on	$-V_{DC}$
on	on	on	off	$+V_{DC}$
on	on	on	on	<b>0</b>

# Modulation Techniques

Example: Sinusoidal PWM (SPWM) in a Five-Level Inverter

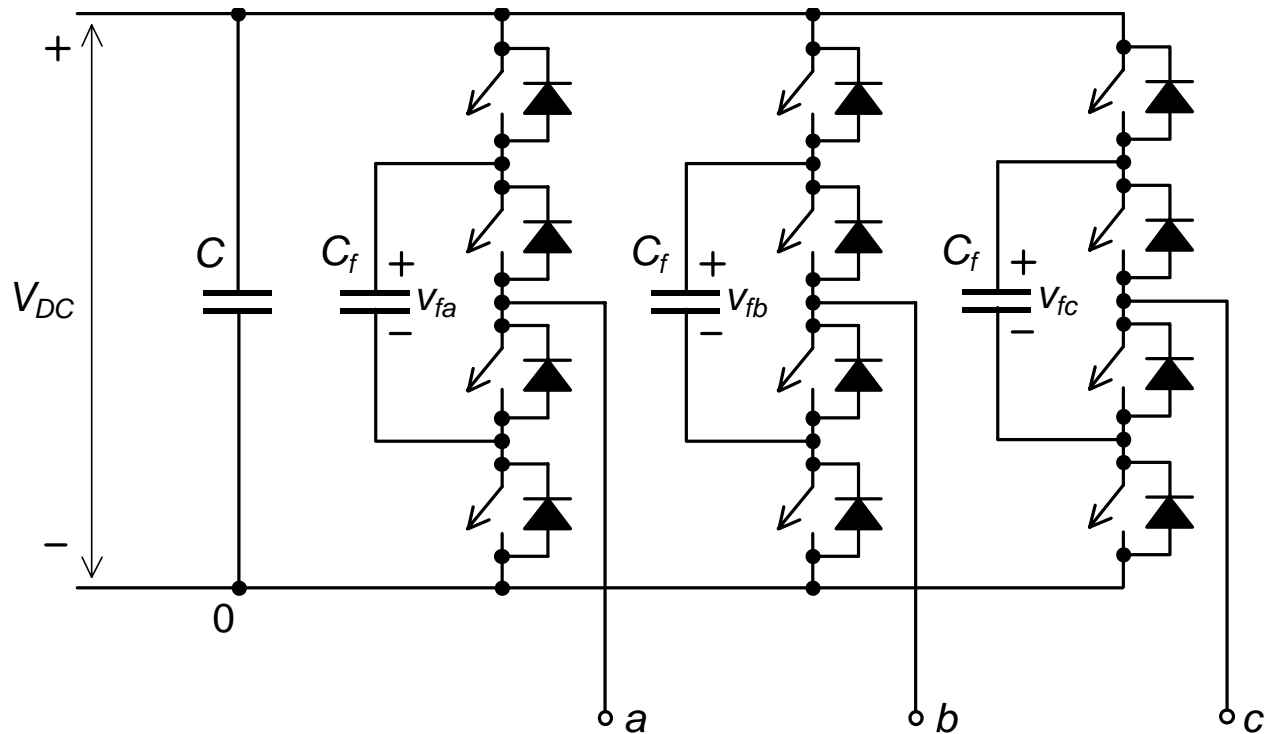


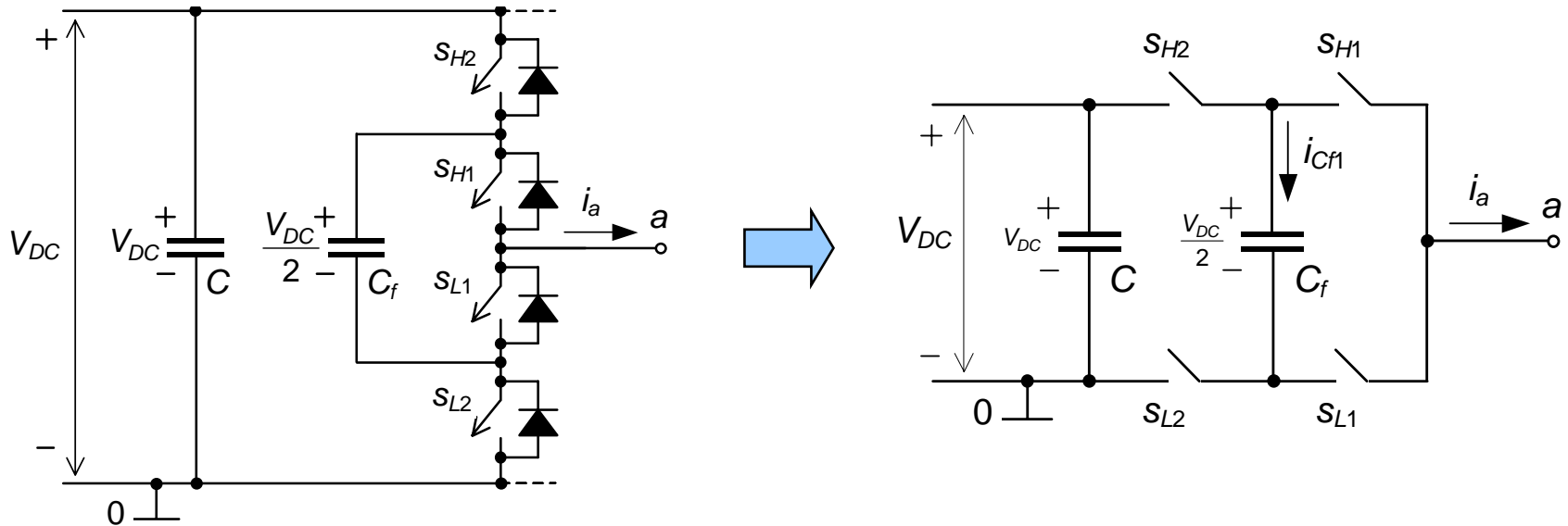


- Modular topologies. Very interesting for practical implementation.
- Main drawback: isolated DC voltage sources are required.
- Isolation is not necessary for applications such as active filtering and reactive compensation. In those cases, capacitors are used to provide DC voltages. Their voltages have to be controlled using redundant states of the converter.
- As many unities as necessary can be connected in cascade. Therefore, any AC voltage level can be achieved.

## (2) Flying-Capacitor (FC) Multilevel Inverter

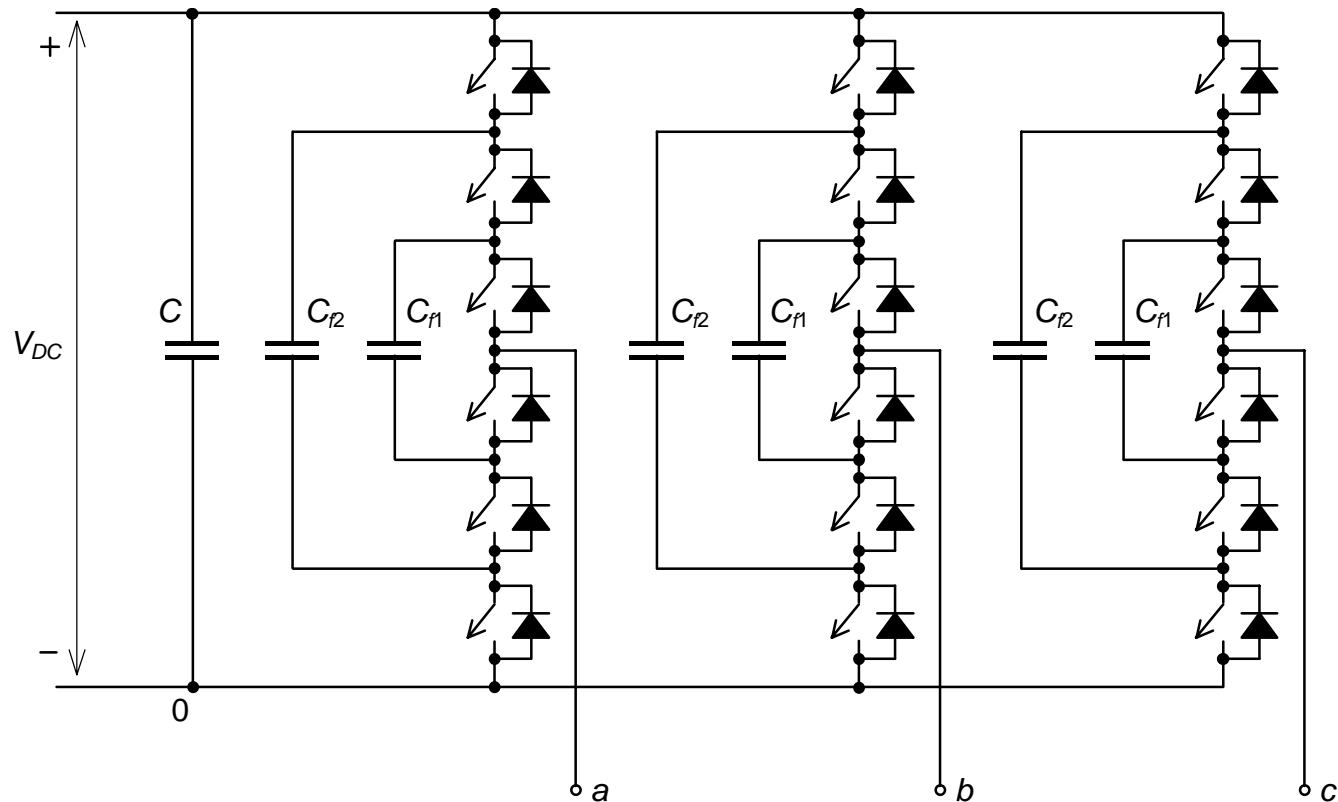
### Three-level Topology



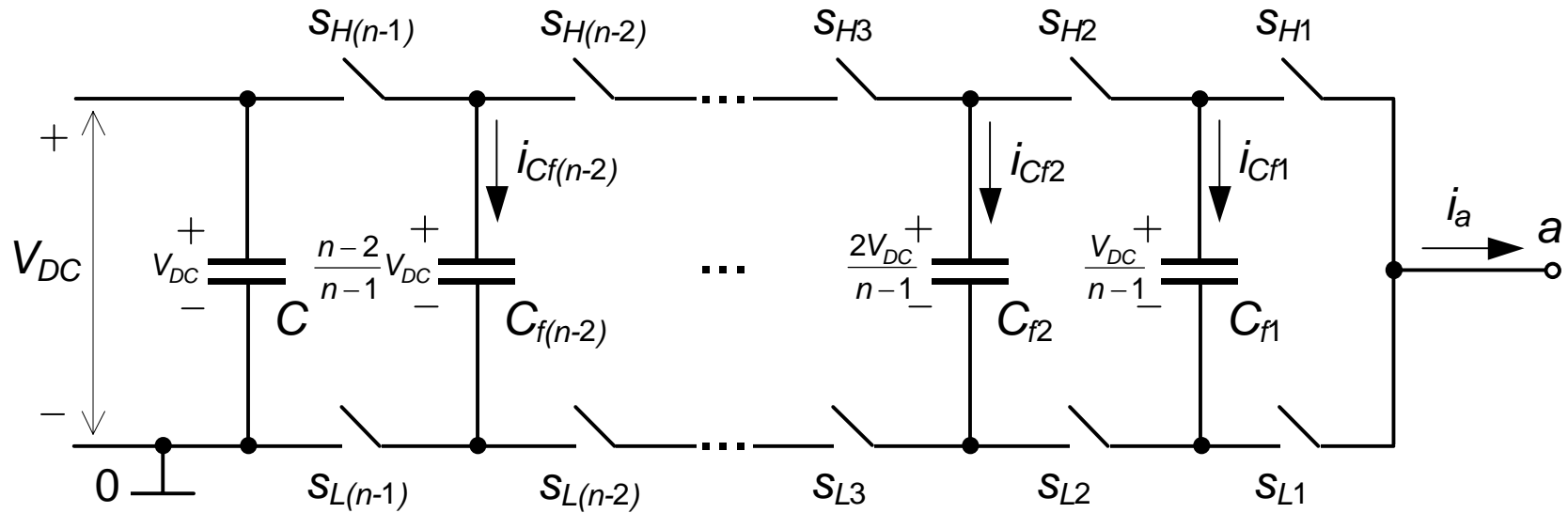


- Each leg of the converter is made up from a set of cells (imbricate cells). The output voltage is synthesized by connecting a number of cells (capacitors) in series.
- $S_{Hi}$  and  $S_{Li}$ , with  $i = \{1, 2\}$ , must be in opposite states to avoid short-circuits.

# FC Four-Level Topology



# Imbricate Cells in an $n$ -level FC Inverter

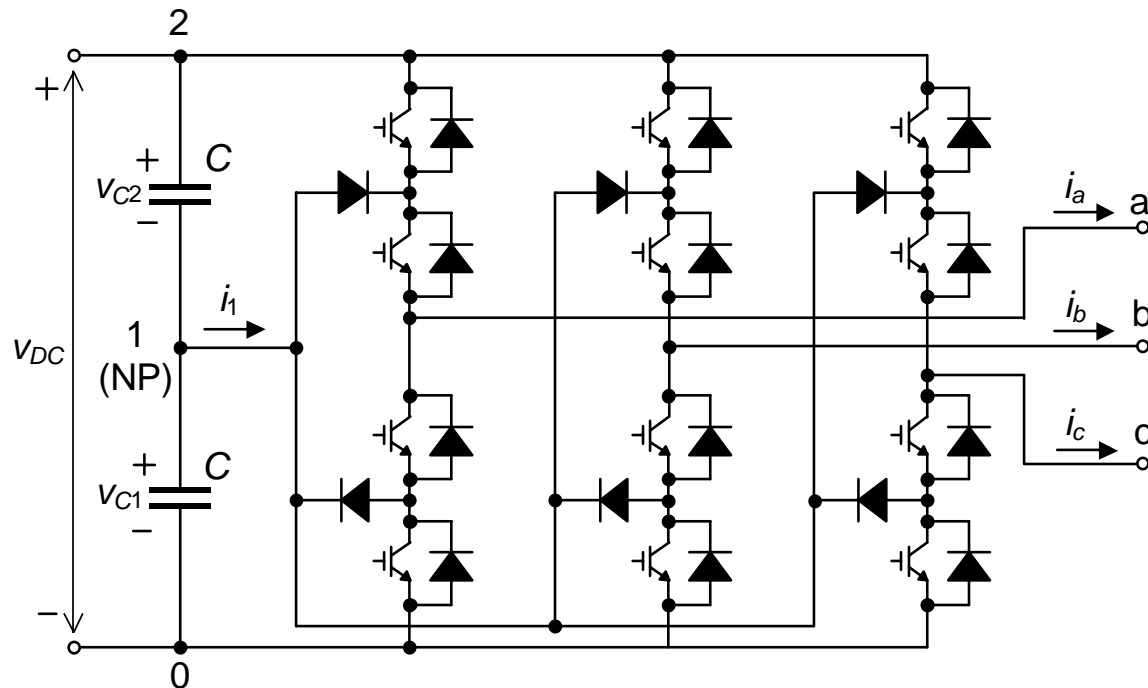


- Voltages on the floating capacitors are different.

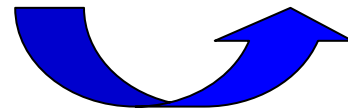
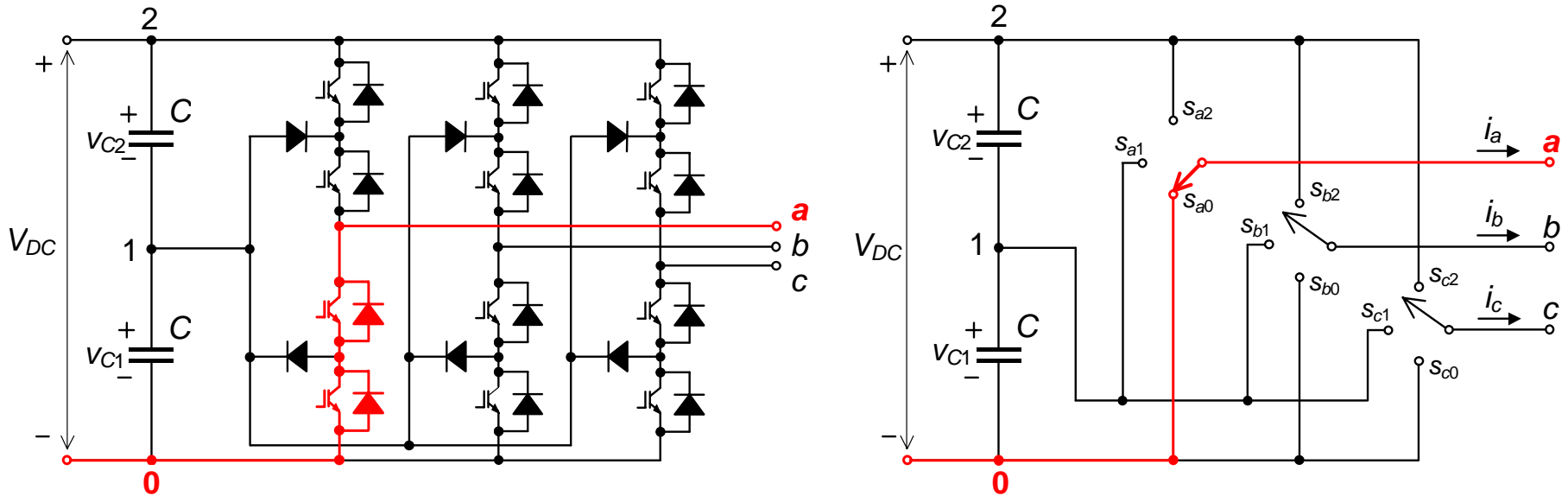
- FC multilevel topologies require a large number of capacitors, specially in high-order structures ( $n > 3$ ).
- Precharge of the flying capacitors is required.
- Voltages on the flying capacitors can be controlled. Each leg regulates the voltages on their capacitors independently of the others.

## (3) Diode-Clamped Inverters

Three-level diode-clamped inverter =  
Neutral-Point-Clamped (NPC) Inverter



## Operation principles

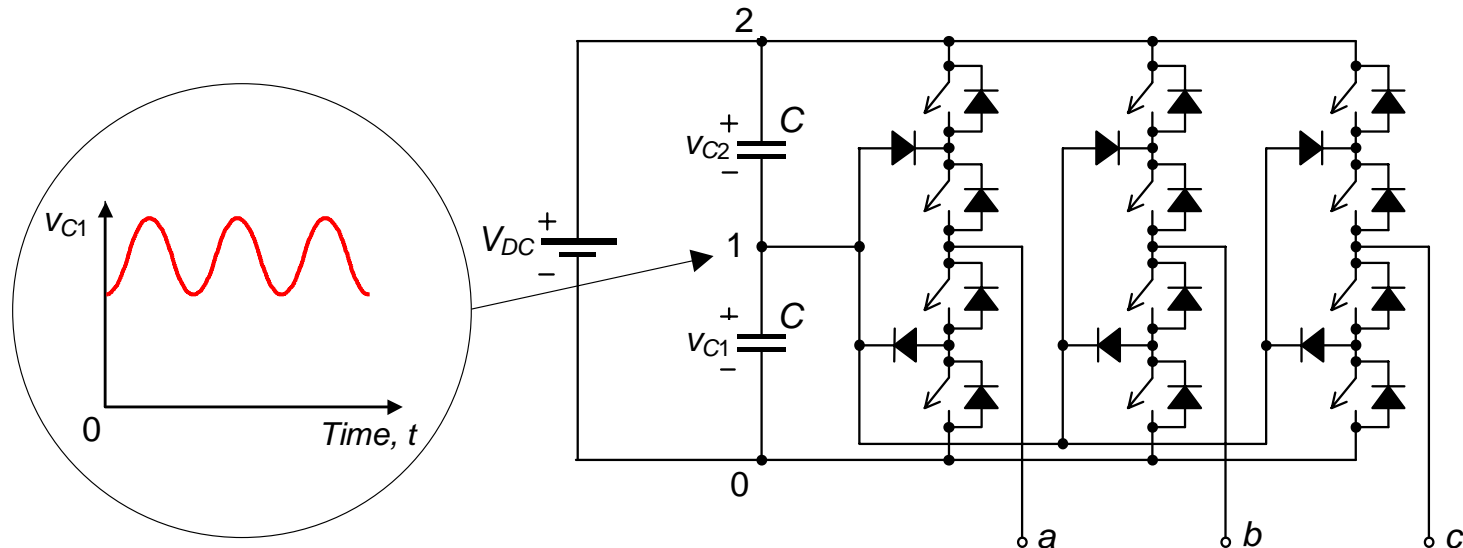


Functional diagram

Two consecutive switches must be in on-state

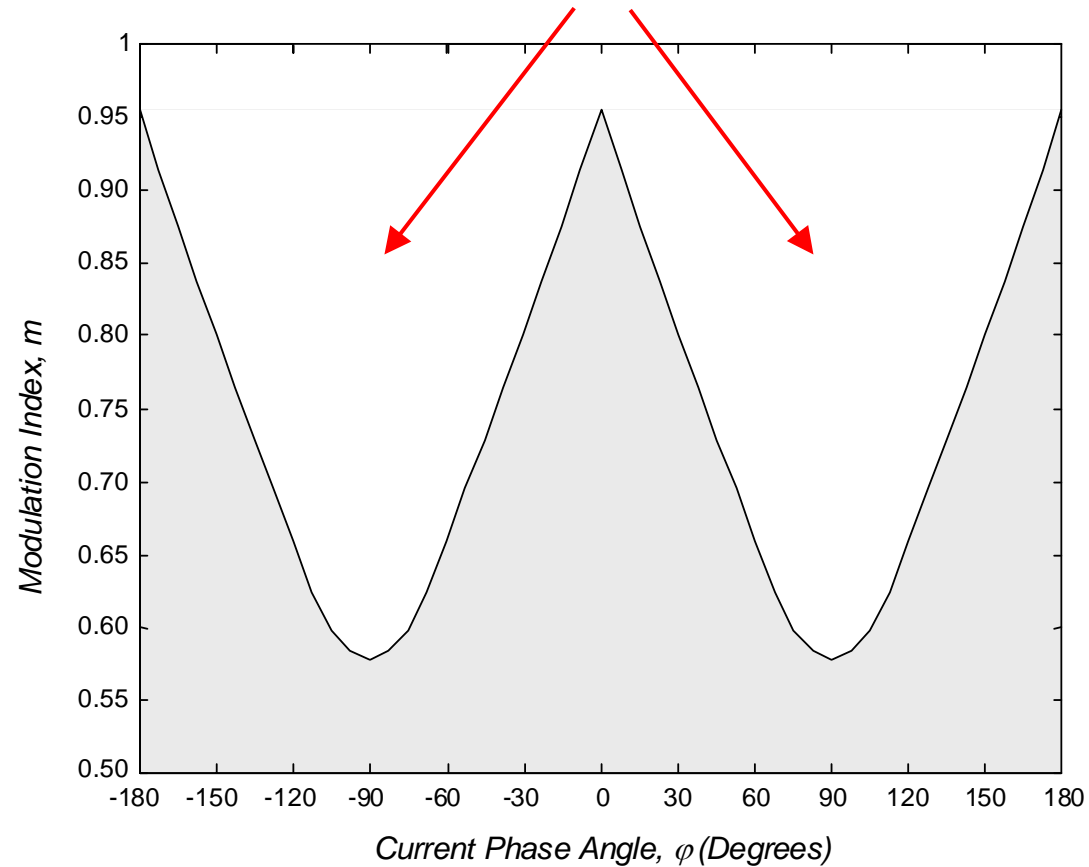


# Neutral-Point Voltage Oscillations



A low-frequency oscillation may appear in the neutral-point (NP) voltage.

## NP Voltage Oscillations

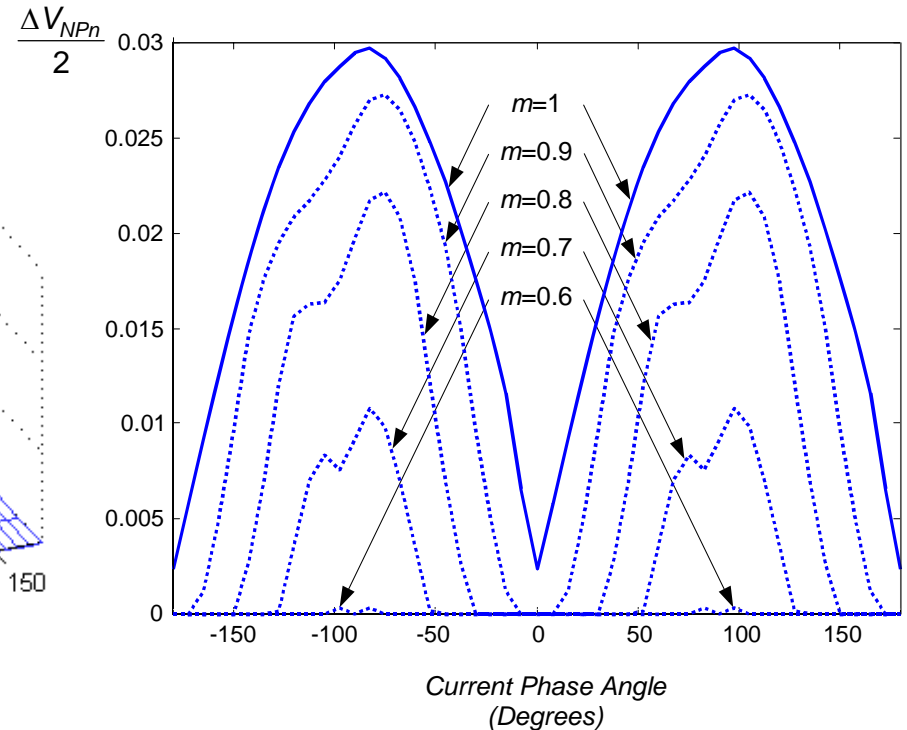
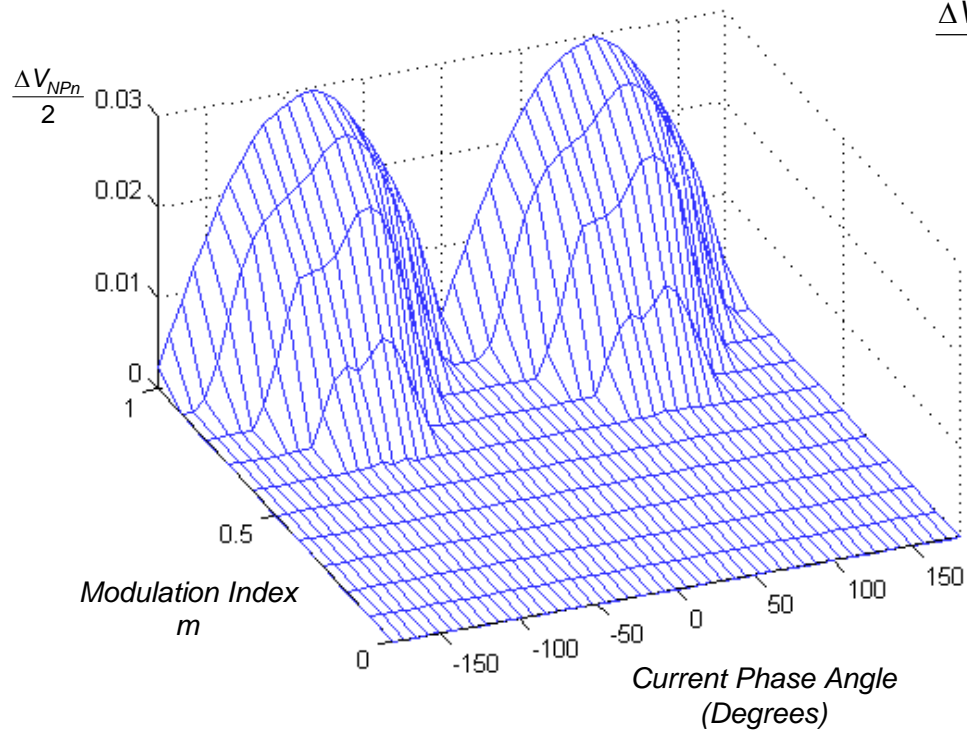


# Voltage Oscillation Amplitude

Normalized amplitude of the NP voltage ripple ( $\Delta V_{NPn}/2$ ):

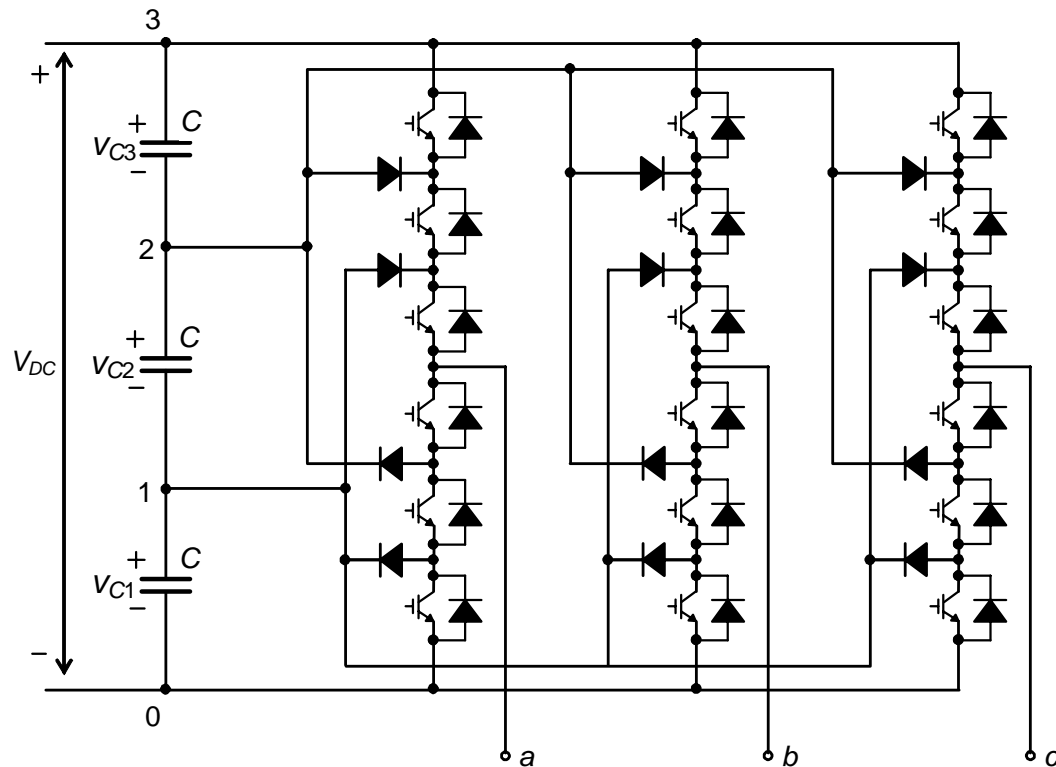
$$\frac{\Delta V_{NPn}}{2} = \frac{\Delta V_{NP}/2}{I_{RMS}/fC}$$

$\Delta V_{NP}/2$  : amplitude of the NP voltage ripple  
 $I_{RMS}$ : RMS output current  
 $f$ : line frequency  
 $C$ : value of the DC-link capacitors



# Four-Level Diode-Clamped Inverter

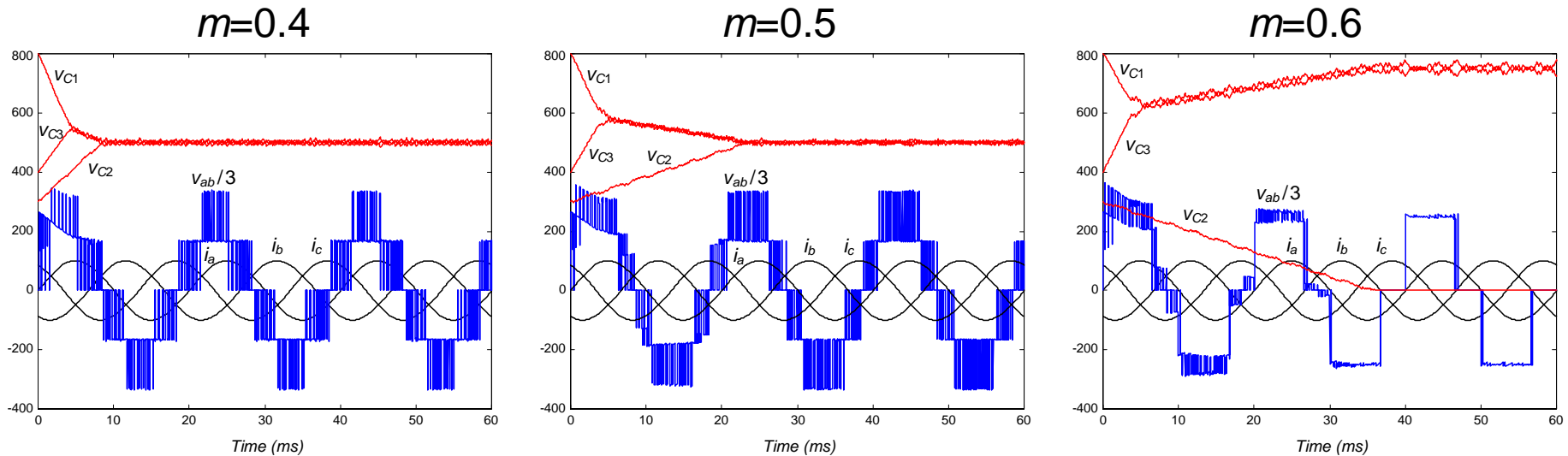
## Four-level topology



# Four-Level Multilevel Inverter

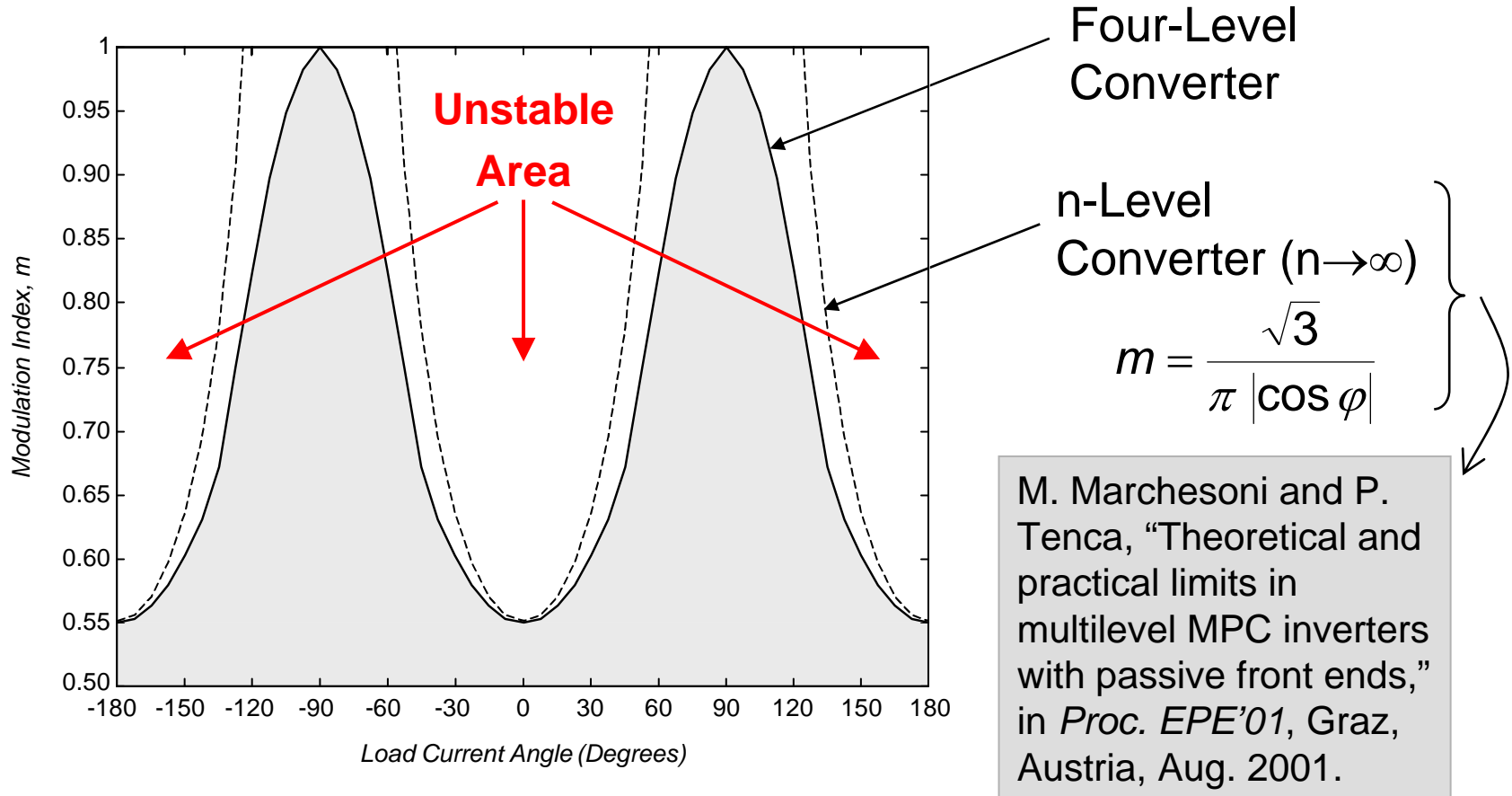
## Voltage balance problems

Example operating under unity power factor



J. Pou, R. Pindado, and D. Boroyevich, "Voltage-Balance Limits in Four-Level Diode-Clamped Converters With Passive Front Ends," *IEEE Trans. Ind. Electron.*, vol. 52, no. 1, pp. 190-196, Feb. 2005.

# Limits of Voltage Balance

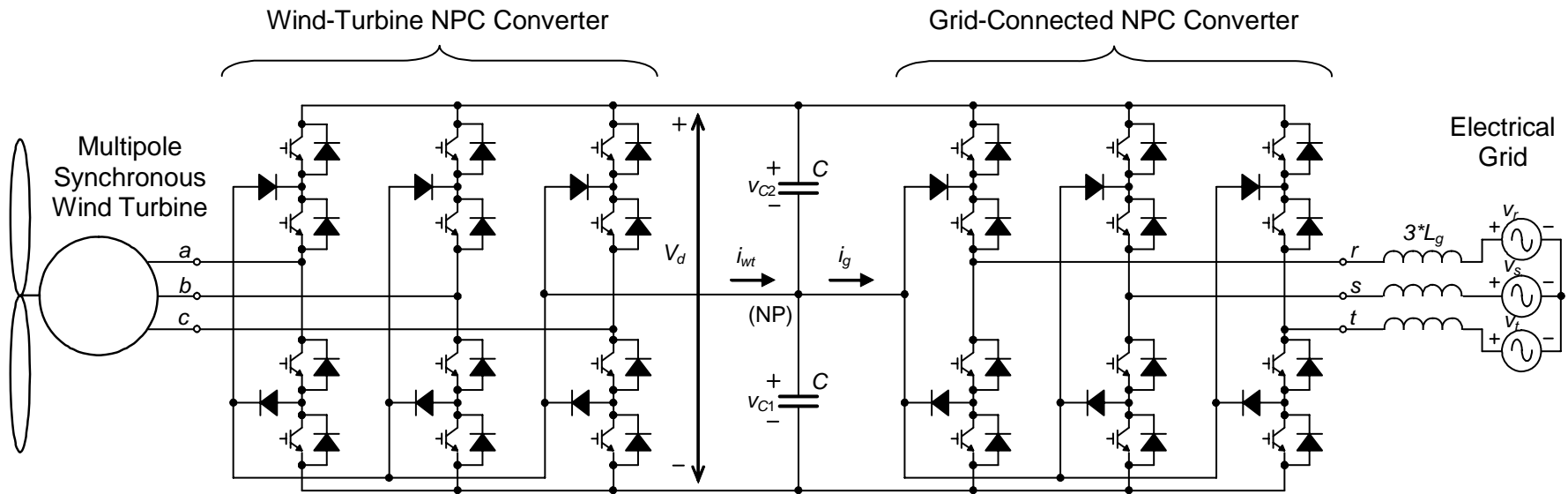


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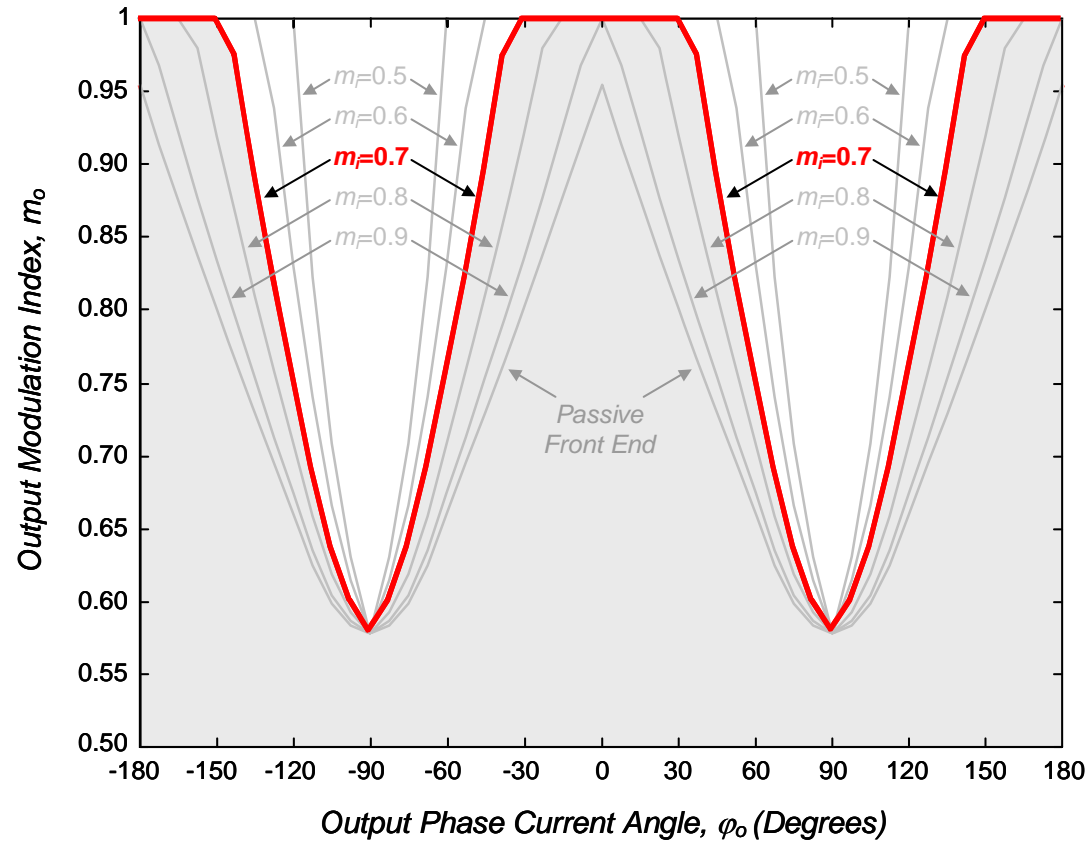
# AC-DC-AC NPC-Based System



- Back-to-back-connected NPC converters. Example of application to MPSCG wind turbines.



# Voltage-balance Improvements

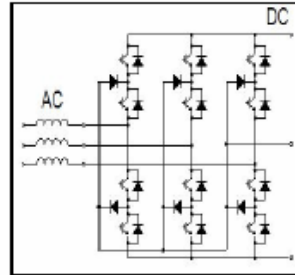


Conditions: constant output current ( $I_{RMSO} = \text{ct.}$ ), unity input power factor ( $\phi_i = 0^\circ, 180^\circ$ ), and 100% efficiency ( $\eta = 1$ ).

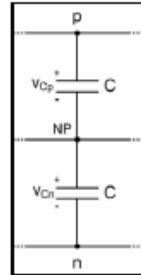
# Matlab-Simulink Simulation Platform



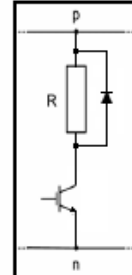
ELECTRICAL GRID



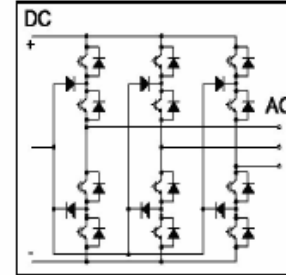
GRID-CONNECTED NPC CONVERTER



DC-LINK CAPACITORS



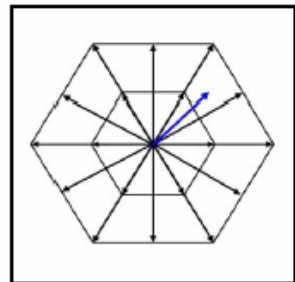
CHOPPER



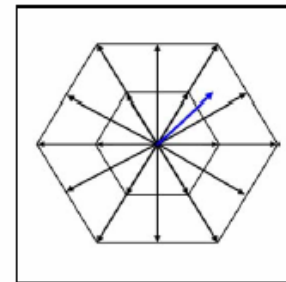
WIND-TURBINE NPC CONVERTER



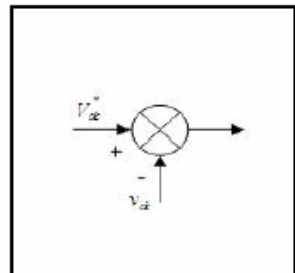
WIND GENERATOR



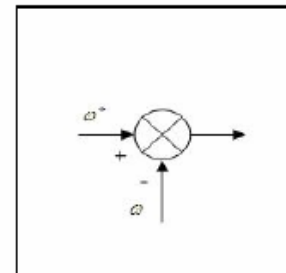
DSPWM for the Grid-Connected NPC Converter



DSPWM for the Wind-Turbine NPC Converter



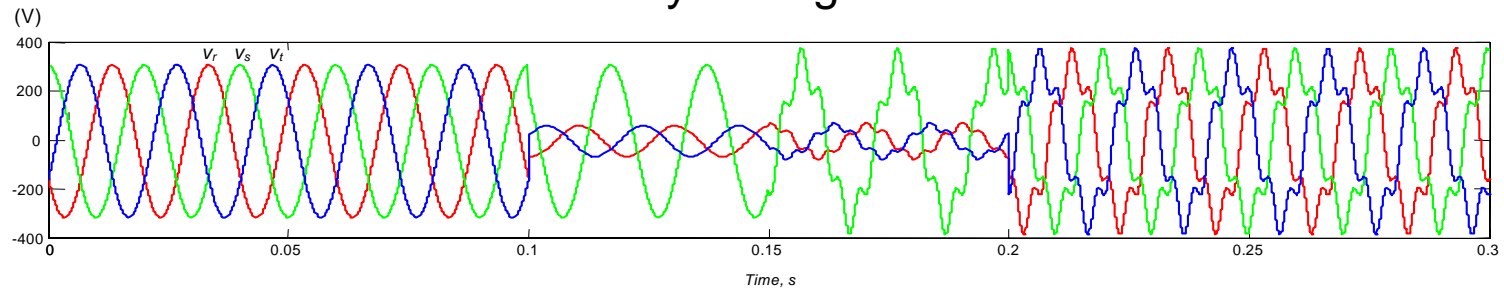
GRID-CONNECTED CONVERTER CONTROL



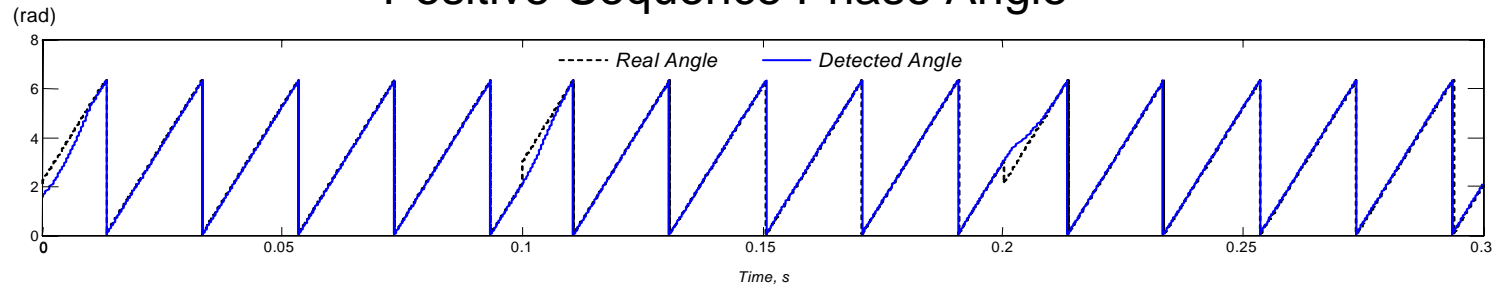
WIND TURBINE CONTROL

## Two-phase voltage dip process with a fifth harmonic

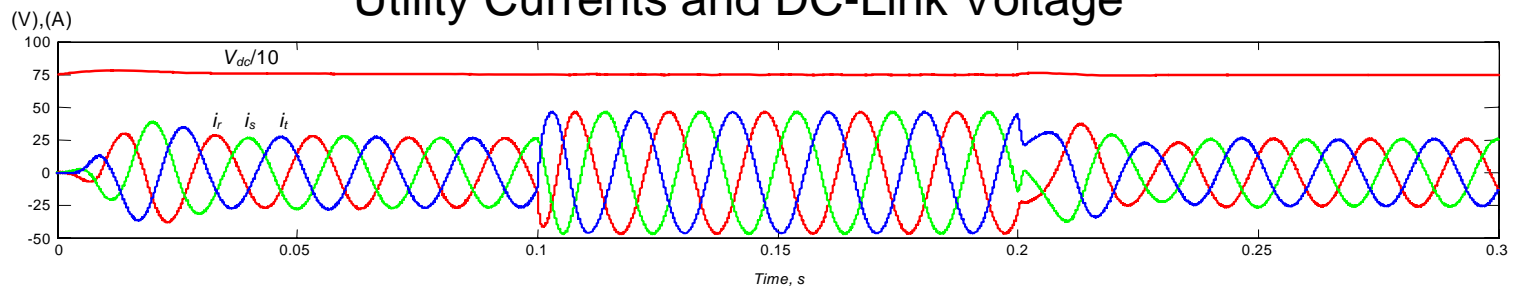
### Utility Voltages



### Positive-Sequence Phase Angle



### Utility Currents and DC-Link Voltage



## Remarks

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- Multilevel topologies can be applied to high-power wind-turbine systems. They are expected to be extensively used when the wind turbines rated power reaches about 10 MW.
- Among the multilevel topologies, the three-level NPC is the most produced used nowadays. An important drawback of this topology is the voltage oscillations that may appear in the NP under some operating conditions.
- The back-to-back connection of NPCs forms an AC/DC/AC system. In such a configuration the NP voltage oscillations become significantly attenuated.